

# Course guide 330061 - M3 - Mathematics III

**Last modified:** 19/05/2023

Unit in charge: Manresa School of Engineering

**Teaching unit:** 749 - MAT - Department of Mathematics.

Degree: BACHELOR'S DEGREE IN CHEMICAL ENGINEERING (Syllabus 2009). (Compulsory subject).

BACHELOR'S DEGREE IN ELECTRICAL ENGINEERING (Syllabus 2009). (Compulsory subject).

BACHELOR'S DEGREE IN INDUSTRIAL ELECTRONICS AND AUTOMATIC CONTROL ENGINEERING (Syllabus

2009). (Compulsory subject).

BACHELOR'S DEGREE IN MECHANICAL ENGINEERING (Syllabus 2009). (Compulsory subject). BACHELOR'S DEGREE IN CHEMICAL ENGINEERING (Syllabus 2016). (Compulsory subject).

BACHELOR'S DEGREE IN INDUSTRIAL ELECTRONICS AND AUTOMATIC CONTROL ENGINEERING (Syllabus

2016). (Compulsory subject).

BACHELOR'S DEGREE IN MECHANICAL ENGINEERING (Syllabus 2016). (Compulsory subject).

BACHELOR'S DEGREE IN MINERAL RESOURCE ENGINEERING AND MINERAL RECYCLING (Syllabus 2021).

(Compulsory subject).

Academic year: 2023 ECTS Credits: 6.0 Languages: Catalan

#### **LECTURER**

Coordinating lecturer: Domenech Blazquez, Margarita

Others: Alsina Aubach, Montserrat

Cors Iglesias, Josep M. Freixas Bosch, Josep

Gimenez Pradales, Jose Miguel Puente Del Campo, M. Albina Rossell Garriga, Josep Maria Rubió Massegú, Josep Samaniego Vidal, Daniel Ventura Capell, Enric

### **DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES**

#### Specific:

1. CE1: Ability to solve mathematical problems that may arise in engineering. Ability to apply knowledge about: linear algebra, geometry, differential geometry, differential and integral calculus, differential and partial differential equations, numerical methods, numerical algorithms, statistics and optimization.

### Transversal:

- 2. EFFICIENT ORAL AND WRITTEN COMMUNICATION Level 2. Using strategies for preparing and giving oral presentations. Writing texts and documents whose content is coherent, well structured and free of spelling and grammatical errors.
- 3. TEAMWORK Level 2. Contributing to the consolidation of a team by planning targets and working efficiently to favor communication, task assignment and cohesion.
- 4. SELF-DIRECTED LEARNING Level 2: Completing set tasks based on the guidelines set by lecturers. Devoting the time needed to complete each task, including personal contributions and expanding on the recommended information sources.



### **TEACHING METHODOLOGY**

In the content exposition sessions, the teacher will introduce the theoretical bases of the subject, concepts, methods and results, illustrating them with suitable examples to facilitate understanding.

The students will have to study independently to assimilate the concepts, solve the proposed exercises either by hand or with the help of the computer.

Face-to-face sessions in small groups where the teacher will solve the doubts that the students have after their autonomous study and there will be practices.

Activities 1, 2 and 3 are part of the small group face-to-face sessions while activity 4 is part of the large group face-to-face sessions.

### **LEARNING OBJECTIVES OF THE SUBJECT**

Learning objectives

On completion of the subject Mathematics III, students must be able to:

- Solve differential equations and Fourier analysis problems with the help of Maple software without difficulties.
- Think in increasingly abstract terms.
- Understand and apply deductive reasoning.
- Organise and apply theoretical knowledge to solve concrete problems.
- Interpret the results obtained with the help of computer tools.

### **STUDY LOAD**

Туре	Hours	Percentage
Hours large group	30,0	20.00
Hours small group	30,0	20.00
Self study	90,0	60.00

Total learning time: 150 h

### **CONTENTS**

## 1. ORDINARY DIFFERENTIAL EQUATIONS.

### **Description:**

- First-order ODEs. Euler method.
- Second-order linear ODEs with constant coefficients. Applications.
- Nth-order homogeneous linear ODEs with constant coefficients.

### **Related activities:**

Test E1 and Activity A1

**Full-or-part-time:** 25h Theory classes: 5h Laboratory classes: 5h Self study: 15h

**Date:** 09/04/2024 **Page:** 2 / 6



### 2. LAPLACE TRANSFORM

### **Description:**

- Definition and properties.
- Inverse transform. Properties.
- Application to solving linear ODEs with constant coefficients and initial conditions.

#### **Related activities:**

Test E1 and Activity A1

Full-or-part-time: 30h Theory classes: 6h Laboratory classes: 6h Self study: 18h

### 3. NUMERICAL SERIES AND FOURIER SERIES

### **Description:**

- Numerical series. Criteria of convergence.
- Fourier series. Dirichlet's theorem.
- Exponential form of the Fourier series. Parseval's identity.

#### **Related activities:**

Test E2 and Activity A2

**Full-or-part-time:** 40h Theory classes: 9h Laboratory classes: 10h Self study: 21h

### 4. FOURIER TRANSFORM

#### **Description:**

- Definition and properties.
- Inverse transform and properties.
- $\hbox{-} {\sf Convolution.}$
- Application to the study of linear systems.

### Related activities:

Test E2 and Activity A2

**Full-or-part-time:** 40h Theory classes: 9h Laboratory classes: 9h Self study: 22h

**Date:** 09/04/2024 **Page:** 3 / 6



### 5. PARTIAL DIFFERENTIAL EQUATIONS

### **Description:**

- Definition and examples.
- Separation of variables and Fourier series to solve PDEs.

#### **Related activities:**

Activity A3

Full-or-part-time: 15h Theory classes: 1h Self study: 14h

### **ACTIVITIES**

### **ACTIVITY A1: DIFFERENTIAL EQUATIONS AND THE LAPLACE TRANSFORM**

#### Description:

An activity that must be carried out individually in the computer room.

### Specific objectives:

On completion of the activity, students must be able to:

- 1. Solve an ordinary differential equation.
- 2. Calculate the Laplace transform of a function.
- 3. Apply the Laplace transform to solve a linear ODE.

#### Material:

Software that is available in the computer room.

Guidelines for practicals, lists of problems and a variety of materials available on ATENEA.

#### Delivery

The assignment must be handed in to the professor.

It must be completed to pass the subject.

It forms part of continuous assessment.

**Full-or-part-time:** 4h Laboratory classes: 1h

Self study: 3h

**Date:** 09/04/2024 **Page:** 4 / 6



### **ACTIVITY A2: FOURIES SERIES AND TRANSFORM**

#### **Description:**

An activity that must be carried out individually in the computer room.

#### Specific objectives:

On completion of the activity, students must be able to:

- 1. Identify whether a numerical series is convergent or divergent.
- 2. Calculate the trigonometric Fourier series of a periodic function.
- 3. Calculate the exponential Fourier series of a periodic function.
- 4. Calculate the Fourier transform of a function.
- 5. Apply the Fourier transform to the study of linear systems.

#### Material:

Software that is available in the computer room.

Guidelines for practicals, lists of problems and a variety of materials available on ATENEA.

#### **Delivery:**

The assignment must be handed in to the professor.

It must be completed to pass the subject.

It forms part of continuous assessment.

Full-or-part-time: 4h Laboratory classes: 1h

Self study: 3h

### **ACTIVITY A3: PARTIAL DIFFERENTIAL EQUATIONS**

#### **Description:**

An activity that must be carried out individually.

### Specific objectives:

On completion of the activity, students must be able to:

1. Solve given temperature distribution and vibration problems using separation of variables.

### Material:

Software that is available in the computer room.

 $\label{lem:condition} \text{Guidelines for practicals, lists of problems and a variety of materials available on ATENEA.}$ 

#### Delivery:

The assignment must be handed in to the professor.

It forms part of continuous assessment.

Full-or-part-time: 3h

Self study: 3h

**Date:** 09/04/2024 **Page:** 5 / 6



#### **ACTIVITY 4: WRITTEN TESTS E1 AND E2**

#### **Description:**

Individual tests in the classroom related to the learning objectives for the subject.

#### Specific objectives:

To assess the general attainment of the objectives of topics 1, 2, 3 and 4

#### Material:

Exam papers (given to students at the exam).

#### **Delivery:**

The answers to the test must be handed in to the professor.

It forms part of continuous assessment.

Full-or-part-time: 16h Theory classes: 4h Self study: 12h

### **GRADING SYSTEM**

The mark is calculated from the NE mark corresponding to Activity 4 and the NA mark corresponding to activities 1, 2 and 3, up to a maximum value of 10 for each one.

The learning objectives are considered to have been met if the final mark for continuous assessment NC=0.7\*NE+0.3\*NA is greater than or equal to 5.

Students with a mark for the subject (NC) of less than 5 may take a final examination (mark: NG).

The student's final mark will be NF=maximum (NC, NG)

# **EXAMINATION RULES.**

All the activities are compulsory.

If students do not carry out one of the activities for the subject, they will be given a mark of 0.

# **BIBLIOGRAPHY**

### Basic:

- Zill, Dennis G. Ecuaciones diferenciales con problemas con valores en la frontera. 9a ed. Cuajimalpa: Cengage Learning, 2018. ISBN 9786075266305.
- Blanchard, Paul; Devaney, R. L.; Hall, Glen R. Differential equations. 4th ed. Pacific Grove: Brooks/Cole, 2011. ISBN 9781133110590.
- Harris, K.; López, R. J. Discovering calculus with Maple. 2nd ed. New York: John Wiley & Sons, 1995. ISBN 0471009733.
- Hsu, Hwei P.; Mehra, R. Análisis de Fourier [on line]. Argentina: Addison-Wesley Iberoamericana, 1987 [Consultation: 03/04/2024]. A v a i l a b l e o n:

 $\frac{https://ebookcentral-proquest-com.recursos.biblioteca.upc.edu/lib/upcatalunya-ebooks/detail.action?pq-origsite=primo&docID=6118\\ \underline{465}. \ ISBN \ 0201029421.$ 

### Complementary:

- Gabel, R. A.; Roberts, R. A. Señales y sistemas lineales. México: Limusa, 1975.

**Date:** 09/04/2024 **Page:** 6 / 6