

## Course guide

# 330137 - MSSD - Modelling and Simulation of Dynamical Systems

Last modified: 04/05/2023

**Unit in charge:** Manresa School of Engineering  
**Teaching unit:** 749 - MAT - Department of Mathematics.

**Degree:** BACHELOR'S DEGREE IN MECHANICAL ENGINEERING (Syllabus 2009). (Optional subject).  
BACHELOR'S DEGREE IN MECHANICAL ENGINEERING (Syllabus 2016). (Optional subject).  
BACHELOR'S DEGREE IN AUTOMOTIVE ENGINEERING (Syllabus 2017). (Optional subject).

**Academic year:** 2023    **ECTS Credits:** 6.0    **Languages:** Catalan, English

## LECTURER

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**Coordinating lecturer:** Cors Iglesias, Josep M.

**Others:**

## PRIOR SKILLS

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For a successful completion of the course, it is convenient to have previously taken the subjects Mathematics I, Mathematics II and Mathematics III.

## DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES

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### Specific:

1. Ability to solve mathematical problems that may arise in engineering. Ability to apply the knowledge of: linear algebra, differential and integral calculus, differential equations, numerical methods, numerical algorithms and optimization

### Transversal:

2. THIRD LANGUAGE. Learning a third language, preferably English, to a degree of oral and written fluency that fits in with the future needs of the graduates of each course.
3. SELF-DIRECTED LEARNING - Level 3. Applying the knowledge gained in completing a task according to its relevance and importance. Deciding how to carry out a task, the amount of time to be devoted to it and the most suitable information sources.

## TEACHING METHODOLOGY

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The large-group sessions (2 hours per week) will be held in the ordinary classroom. In these sessions the main methods and theoretical content will be presented. The small-group sessions (2 hours per week) will be held in the computer room, and will be mainly focused on the usage of Matlab as a simulation tool.

## LEARNING OBJECTIVES OF THE SUBJECT

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At the end of the course, students have to be able to:

- Formulate suitable mathematical models for different types of dynamical systems.
- Use of Matlab as a tool to simulate dynamical systems.
- Compute numerically the main objects of a dynamical system: periodic orbits, invariant manifolds,...



## STUDY LOAD

Type	Hours	Percentage
Self study	90,0	60.00
Hours large group	30,0	20.00
Hours small group	30,0	20.00

**Total learning time:** 150 h

## CONTENTS

### Unit 1: Mathematical modelling of dynamical systems.

**Description:**

Mathematical models. First-order linear ODE models. General first-order ODE models. Higher-order ODE models.

**Specific objectives:**

Review of the main elements of mathematical modelling for dynamical systems with lumped parameters.

**Related activities:**

Activity A1.

**Full-or-part-time:** 20h

Theory classes: 4h

Laboratory classes: 4h

Self study : 12h

### Unit 2: Numerical tools

**Description:**

Introduction to numerical methods.

**Specific objectives:**

Presentation of the main concepts and methods for numerical ODE solving.

**Related activities:**

Activity A1.

**Full-or-part-time:** 40h

Theory classes: 8h

Laboratory classes: 8h

Self study : 24h

### Unit 3: Mechanical vibrations.

**Description:**

Mass-spring model. Mass-spring-damper model. Resonance. Multi-degree-of-freedom oscillators.

**Specific objectives:**

Study and discussion of various dynamical models of mechanical oscillators and their numerical simulation.

**Related activities:**

Activity A2.

**Full-or-part-time:** 40h

Theory classes: 8h

Laboratory classes: 8h

Self study : 24h

### Unit 4: Introduction to Chaos

**Description:**

Periodic forcing of nonlinear system and chaos.

**Related activities:**

Activity A3.

**Full-or-part-time:** 30h

Theory classes: 6h

Laboratory classes: 6h

Self study : 18h

### Unit 5: Introduction to Simulink

**Description:**

To model, simulate, and analyze dynamical systems using Simulink

**Related activities:**

Activity A2.

**Full-or-part-time:** 20h

Theory classes: 4h

Laboratory classes: 4h

Self study : 12h

## ACTIVITIES

### Activity A1: Computing periodic orbits in first-order equations

**Description:**

To compute periodic orbits using numerical tools.

**Full-or-part-time:** 8h

Self study: 8h

### Activity A2: Numerical simulation of mechanical vibrations.

**Description:**

Application of the basic concepts of mechanical vibrations. Numerical modelling and simulation of mechanical oscillators with Matlab and Simulink.

**Full-or-part-time:** 8h

Self study: 8h

### Activity A3: Chaos

**Description:**

Poincaré sections for a mechanical systems with a periodic forcing.

**Full-or-part-time:** 8h

Self study: 8h

## GRADING SYSTEM

The course follows a continuous assessment system, which produces a course mark  $CM = 1/3 * (M1 + M2 + M3)$ , where  $M_j$ ,  $j = 1, 2, 3, 4$ , represents the mark obtained in the activity  $A_j$ . The course objectives will be considered achieved if CM is at least 5. Students who have completed the evaluation activities and obtain a course mark CM less than 5 can take a global exam. Students who pass that global exam will obtain a final grade of Pass 5; otherwise, they will keep their course mark (CM) as final grade.

Reevaluation: In this course there is a reevaluation procedure. Students who have obtained a failing grade in the ordinary assessment period can access the reevaluation process (students with a not-attended grade cannot access the reevaluation process). The reevaluation scheme consists in a new examination that takes place in the reevaluation period (at the end of June or the beginning of July). The reevaluation exam includes all the course material and produces a pass /fail outcome. Students who achieve a pass grade in the reevaluation exam will be awarded a final course mark of 5; otherwise, they will keep the grade obtained in the ordinary assessment process.

## EXAMINATION RULES.

All evaluation activities are compulsory. A zero mark will be obtained in not-attended activities. Whenever possible, evaluation activities will be carried out in person. In online and homemade evaluation activities, when deemed appropriate, the authorship of the presented exams/reports will be validated by means of an additional questionnaire and / or a personal interview (online or in person).

## BIBLIOGRAPHY

**Basic:**

- Klee, Harold. Simulation of dynamic systems with MATLAB and Simulink. Boca Raton, FL: CRC Press, cop. 2007. ISBN 9781420044188.
- Lynch, Stephen. Dynamical systems with applications using MATLAB [on line]. Boston [etc.]: Birkhäuser, cop. 2004 [Consultation: 29/01/2024]. Available on: <https://link-springer-com.recursos.biblioteca.upc.edu/book/10.1007/978-3-319-06820-6>. ISBN 0817643214.
- Bonet, Carles. Càlcul numèric [on line]. Barcelona: Edicions UPC, 1994 [Consultation: 27/07/2022]. Available on: <https://upcommons.upc.edu/handle/2099.3/36356>. ISBN 8476533764.
- Blanchard, Paul; Devaney, Robert L; Hall, Glen R; Persaud, Brian. Differential equations. 4th ed., International ed. Pacific Grove: Brooks/Cole, cop. 2011. ISBN 9781133110590.

## RESOURCES

**Other resources:**

Notes and / or slides related to the theoretical and practical classes.

List of problems.