

# Course guide 240131 - 240131 - Differential Equations

Last modified: 16/05/2023

Unit in charge: Teaching unit:	Barcelona School of Industrial Engineering 749 - MAT - Department of Mathematics.	
Degree:	BACHELOR'S DEGREE IN I	NDUSTRIAL TECHNOLOGY ENGINEERING (Syllabus 2010). (Compulsory subject).
Academic year: 2023	ECTS Credits: 6.0	Languages: Catalan, Spanish

# LECTURER

Coordinating lecturer: PERE GUTIERREZ SERRES

Others:

# **DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES**

### Specific:

1. Capacity to solve mathematical problems that can appear in engineering . Aptitude to apply knowledge about: linear algebra; geometry; differential geometry; differential and integral calculus; differential equations and derived partial equations; numerical methods; numerical algorithm; statistics and optimisation.

# **TEACHING METHODOLOGY**

There are 2 hours per week of "magistral lectures" (exposition of theoretical aspects), and 2 hours per week of "problem solving".

# LEARNING OBJECTIVES OF THE SUBJECT

At the end of the course, students should be able:

- \* to apply the fundamental theorems of Vector Calculus
- \* to solve, classify and draw the phase portrait of 2D and 3D systems of linear ODEs with constant coefficients
- $\ast$  to use the tools to determine the stability in some systems of nonlinear ODEs
- \* to solve some basic PDEs (wave, heat, Laplace/Poisson, etc)
- \* to use sofware in order to obtain numerical approximations in problems from the previous items

### STUDY LOAD

Туре	Hours	Percentage
Hours large group	60,0	40.00
Self study	90,0	60.00

Total learning time: 150 h



# CONTENTS

### **Vector Calculus**

### **Description:**

Line and surface integration of functions and vector fields. Integral theorems: Newton\_Leibniz, Green, Gauss and Stokes.

#### **Related competencies :**

CE1. Capacity to solve mathematical problems that can appear in engineering . Aptitude to apply knowledge about: linear algebra; geometry; differential geometry; differential and integral calculus; differential equations and derived partial equations; numerical methods; numerical algorithm; statistics and optimisation.

### Full-or-part-time: 65h

Theory classes: 13h Practical classes: 13h Self study : 39h

### **Ordinary Differential Equations (ODEs)**

#### **Description:**

Initial and boundary value problems. Stability and classification of linear systems with constant coefficients. Stability of nonlinear systems. Modeling.

#### **Related competencies :**

CE1. Capacity to solve mathematical problems that can appear in engineering . Aptitude to apply knowledge about: linear algebra; geometry; differential geometry; differential and integral calculus; differential equations and derived partial equations; numerical methods; numerical algorithm; statistics and optimisation.

#### Full-or-part-time: 60h

Theory classes: 12h Practical classes: 12h Self study : 36h

### **Partial Differential Equations (PDEs)**

### **Description:**

Wave, heat and Laplace/Poisson equations. Conservation laws. D'Alembert formula. Separation of variables.

#### **Related competencies :**

CE1. Capacity to solve mathematical problems that can appear in engineering . Aptitude to apply knowledge about: linear algebra; geometry; differential geometry; differential and integral calculus; differential equations and derived partial equations; numerical methods; numerical algorithm; statistics and optimisation.

# Full-or-part-time: 25h Theory classes: 5h

Practical classes: 5h Self study : 15h

### **GRADING SYSTEM**

A partial exam (EP), a final exam (EF) and a practice exam (M). The final score is 0.35\*EP+0.55\*EF+0.1\*M. The reevaluation exam (R) is a single test and its score replaces the previous EP and EF scores, and hence the final score, in this case, becomes 0.9\*R+0.1\*M (to be maximized with the final score previously obtained).



# **EXAMINATION RULES.**

In the partial and final exams, only a sheet made by oneself can be used. For the practice exam, the allowed material will previously be announced. The use of a calculator, a primitive table or other tables, and (of course) mobile phones or similar devices is not allowed. Changes of group are not allowed.

# **BIBLIOGRAPHY**

### **Basic:**

- P. Pascual (ed.) et al. Càlcul integral per a enginyers [on line]. Barcelona: UPC, 2002 [Consultation: 07/04/2017]. Available on: http://hdl.handle.net/2099.3/36742. ISBN 8483016273.

- Zill, Dennis G.. Ecuaciones diferenciales con aplicaciones de modelado. 11ª ed.. México DF: Cengage Learning Editores, 2018. ISBN 9786075266312.

### **Complementary:**

- Quarteroni, Alfio, F. Saleri. Cálculo científico con MATLAB y Octave [on line]. Milano: Springer, 2006 [Consultation: 15/06/2018]. Available on: <u>http://dx.doi.org/10.1007/978-88-470-0504-4</u>. ISBN 9788847005037.

- Marsden, Jerrold E. ; A.J. Tromba. Cálculo vectorial. 6ª ed.. Madrid: Pearson, 2018. ISBN 9788490355787.

- R. Larson i B.H. Edwards. Cálculo 2 de varias variables [on line]. 9<sup>a</sup> ed.. México DF: McGraw-Hill, 2010 [Consultation: 19/10/2020]. Available on: <u>http://www.ingebook.com/ib/NPcd/IB\_BooksVis?cod\_primaria=1000187&codigo\_libro=5686</u>. ISBN 9789701071342.

- R.L. Borrelli i C.S. Coleman. Ecuaciones diferenciales : una perspectiva de modelación. México: Oxford Univ. Press, 2002. ISBN 9706136118.

- M. Tenenbaum i H. Pollard. Ordinary differential equations. New York: Dover, 1985. ISBN 0486649407.

## **RESOURCES**

Other resources: https://mat-web.upc.edu/etseib/ed/