

## Course guide

### 390109 - FM2 - Mathematics II

**Last modified:** 03/06/2024

**Unit in charge:** Barcelona School of Agri-Food and Biosystems Engineering  
**Teaching unit:** 749 - MAT - Department of Mathematics.

**Degree:** BACHELOR'S DEGREE IN BIOSYSTEMS ENGINEERING (Syllabus 2009). (Compulsory subject).  
BACHELOR'S DEGREE IN FOOD ENGINEERING (Syllabus 2009). (Compulsory subject).  
BACHELOR'S DEGREE IN AGRONOMIC SCIENCE ENGINEERING (Syllabus 2018). (Compulsory subject).

**Academic year:** 2024    **ECTS Credits:** 6.0    **Languages:** Catalan, Spanish

#### LECTURER

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**Coordinating lecturer:** Boza Rocho, Santiago

**Others:** Boza Rocho, Santiago  
Castañar Cañas, Jose Manuel  
Garcia Martinez, Yamila  
Ginovart Gisbert, Marta  
Pelayo Melero, Ignacio Manuel  
Saseta Ibáñez, Federico

#### DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES

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**Specific:**

2. Fundamentals of computer use and programming, operating systems, data bases, software for engineering applications.
3. Ability to solve mathematic problems in an engineering context . Ability to apply the knowledge of integral calculus, differential equations, numeric methods, numeric algorithms,

**Generical:**

1. Ability to solve problems.

#### TEACHING METHODOLOGY

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The course topics are released on one-hour and two-hour lectures. In the lectures students' involvement is encouraged by means of the performance of low-stake activities in the classroom, such as asking-answering questions regarding one lecture, students presentations on specific topics, or the solving of exercises and problems related to the topics taught.

The solving of exercises and problems will be performed primarily in small groups and computer labs. In these sessions students will be asked to seek appropriate solutions through the application of formulae or algorithms, the implementation of procedures to transform the available information, the interpretation of results and the use of appropriate software in the computer lab sessions.

Autonomous learning will focus on key actions aimed at solving exercises and problems. Several quizzes will be performed as self-learning activities, available on the virtual campus. There will be a written mid-semester exam. A written final global exam will be held at the end of the course.

## LEARNING OBJECTIVES OF THE SUBJECT

The subject Mathematics II addresses general formative purposes. It aims to generate learning skills and to promote the assessment of the power and usefulness of mathematical models and procedures, in order to understand and to make decisions in the techno-scientific area. Mathematics plays a fundamental role in helping to understand the techno-scientific environment and to deal with it in an autonomous and creative way. As in all the areas of mathematics, systematic and constant work, accurate reasoning and interpretation, and abstraction will be enhanced throughout the teaching-learning process.

By the end of the course the student will be able to carry out logical reasoning, to develop analytical and critical thinking, to evaluate arguments rigorously and to communicate them effectively.

The course is structured into three core topics: 1) integral calculus, 2) differential equations, and 3) numerical methods and programming. Throughout the course the emphasis is placed on problem solving and applications to branches of engineering and science.

In the area of integral calculus students will achieve fundamental concepts relating to comprehensive, and also resolve with basic methods exercises related to these applications in the case of real functions of real variable. In the area of differential equations, the purpose will be that students work with the practical aspects of solving ordinary differential equations, giving priority to applications in other branches of science and technology. Regarding partial differential equations, students get a brief overview of what they are and their use. Regarding numerical methods, the student will be introduced in the basic numerical techniques and the use of certain specific methods. Regarding the area of programming and applications students will use worksheets and specific programs to solve complex mathematical problems.

## STUDY LOAD

Type	Hours	Percentage
Hours small group	20,0	13.33
Self study	90,0	60.00
Hours large group	40,0	26.67

**Total learning time:** 150 h

## CONTENTS

### INTEGRAL CALCULUS

#### Description:

0. Complex numbers.

1.1. Antiderivative (indefinite integral): definition, non-uniqueness, notation. Basic antiderivatives. Rules for antiderivation: linearity. Integration by parts, by substitution, by partial fractions.

1.2. Definite integrals (proper integrals): definition, calculation methods. Connection with surface areas.

1.3. Improper integrals: definitions. Types of improper integrals. Convergence. Connection with surface areas

#### Related activities:

Activity 1: Lectures.

Activity 2: Individual written.

Activity 3: Problem and exercise solving.

Activity 4: Computer Lab Sessions.

Activity 5: Questionnaires

#### Full-or-part-time: 44h

Theory classes: 12h

Laboratory classes: 2h

Self study : 30h

## DIFFERENTIAL EQUATIONS

### Description:

- 2.1. Ordinary differential equations (ODEs). Definitions and basic concepts. Separable ordinary differential equations. Homogeneous ordinary differential equations. First-order linear ordinary differential equations. Second-order linear ordinary differential equations with constant coefficients.
- 2.2. Systems of first-order linear ordinary differential equations with constant coefficients.
- 2.3. Partial differential equations.

### Related activities:

- Activity 1: Lectures.
- Activity 2: Individual written test.
- Activity 3: Problem and exercise solving.
- Activity 4: Computer Lab Sessions.
- Activity 5: Questionnaires

### Full-or-part-time: 50h

Theory classes: 14h

Laboratory classes: 6h

Self study : 30h

## NUMERICAL METHODS AND PROGRAMMING

### Description:

- 3.1. Numerical methods. Numerical solution of equations (one and several variables). Numerical integration. Numerical solution of differential equations.
- 3.2. Programming and applications.

### Related activities:

- Activity 1: Lectures.
- Activity 2: Individual written test.
- Activity 3: Problem and exercises solving.
- Activity 4: Computer Lab Sessions.
- Activity 5: Questionnaires

### Full-or-part-time: 56h

Theory classes: 14h

Laboratory classes: 12h

Self study : 30h

## ACTIVITIES

### ACTIVITY 1. LECTURES

### Full-or-part-time: 97h

Theory classes: 38h

Self study: 59h



## ACTIVITY 2. INDIVIDUAL WRITTEN TEST

**Material:**

Calculator. One formulae sheet.

**Delivery:**

Mid-term exam: 30% of the final grade.

Final exam: 45% of the final grade.

**Full-or-part-time:** 2h

Theory classes: 2h

## ACTIVITY 3. EXERCISES AND PROBLEM SOLVING

**Material:**

Course material available at Atenea.

**Full-or-part-time:** 20h

Laboratory classes: 10h

Self study: 10h

## ACTIVITY 4. COMPUTER LAB SESSIONS

**Material:**

Course material available at Atenea.

**Full-or-part-time:** 15h

Laboratory classes: 10h

Self study: 5h

## ACTIVITY 5: QUESTIONNAIRES

**Description:**

Individual, distance learning activity. Each questionnaire takes at most two hours.

**Material:**

Available at the virtual campus Atenea.

**Delivery:**

5% of the final grade.

**Full-or-part-time:** 16h

Self study: 16h

## GRADING SYSTEM

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N1: The continuous assessment will be developed mainly in the context of small groups and computer lab sessions.

N2: There will be several questionnaires throughout the course.

N3: There will be a mid-semester written exam.

N4: There will be a final (global) written exam at the end of the semester.

The final mark (Nfinal) will be computed as follows:

$$N_{\text{final}} = 0.20 N_1 + 0.05 N_2 + 0.30 N_3 + 0.45 N_4$$

Students who fail to pass the course can sit for the written exams N3 and N4 in the reassessment exam period.

## BIBLIOGRAPHY

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### Basic:

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- Gerald, C.F.; Wheatley, P.O. Análisis numérico con aplicaciones. 6a ed. Mèxic: Pearson Educación, 2000. ISBN 9684443935.
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### Complementary:

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- Gibergans Bàguena, Josep. Matemáticas para la ingeniería con Maple. Barcelona: Edicions UPC, 2008. ISBN 9788483019672.
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