

# Course guide 270633 - SNM - Stochastic Network Modelling

Last modified: 13/07/2022

Unit in charge: Teaching unit:	Barcelona School of Informatics 701 - DAC - Department of Computer Architecture.	
Degree:	MASTER'S DEGREE IN INNOVATION AND RESEARCH IN INFORMATICS (Syllabus 2012). (Optional subject).	
Academic year: 2022	ECTS Credits: 6.0 Languages: English	
LECTURER		
Coordinating lecturer:	LLORENÇ CERDÀ ALABERN	
Others:	Primer quadrimestre: LLORENÇ CERDÀ ALABERN - 10	

# **PRIOR SKILLS**

Probability, random variables and distribution (continuous and discrete) algebra: systems of equations, determinant, eigenvalues  $\Box$  and eigenvectors, diagonalization.

## **DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES**

## Specific:

CEE2.1. Capability to understand models, problems and algorithms related to distributed systems, and to design and evaluate algorithms and systems that process the distribution problems and provide distributed services.

CEE2.2. Capability to understand models, problems and algorithms related to computer networks and to design and evaluate algorithms, protocols and systems that process the complexity of computer communications networks.

CEE2.3. Capability to understand models, problems and mathematical tools to analyze, design and evaluate computer networks and distributed systems.

## Generical:

CG1. Capability to apply the scientific method to study and analyse of phenomena and systems in any area of Computer Science, and in the conception, design and implementation of innovative and original solutions.

CG3. Capacity for mathematical modeling, calculation and experimental designing in technology and companies engineering centers, particularly in research and innovation in all areas of Computer Science.

#### Transversal:

CTR6. REASONING: Capacity for critical, logical and mathematical reasoning. Capability to solve problems in their area of study. Capacity for abstraction: the capability to create and use models that reflect real situations. Capability to design and implement simple experiments, and analyze and interpret their results. Capacity for analysis, synthesis and evaluation.

## **TEACHING METHODOLOGY**

There will be 4 hours per week, dedicated to theoretical classes to explain the theory and solve problems. The students' activities will consist of reading material and solving practical problems that will be proposed at each theoretical unit. The problems will be collected and corrected during the course. There will be research oriented problems to be solved using numerical tools as MATLAB.



# LEARNING OBJECTIVES OF THE SUBJECT

2.Being able to model a process that evolves over time with a discrete and continuous time Markov chain

3.Being able to compute the steady state and transient solution of a Markov chain

4.Being able to model processes that engage the formation of queues

5.Being able to resolve the basic queues: M/M/1, M/G/1, M/G/1/K

# **STUDY LOAD**

Туре	Hours	Percentage
Self study	96,0	64.00
Hours large group	54,0	36.00

## Total learning time: 150 h

# CONTENTS

Introduction

#### Description:

Concept of probability space, sequence of random variables and stochastic processes.

## **Discrete Time Markov Chains (DTMC)**

#### **Description:**

Definition of a DTMC, Transient Solution, Classification of States, Steady State, Finite Absorbent Chains

## Continuous Time Markov Chains (CTMC)

#### **Description:**

Definition of a CTMC, Transient Solution, Steady State, Semi-Markov Process and Embedded MC, Finite Absorbent Chains

#### **Queuing Theory**

#### **Description:**

Kendal Notation, Little Theorem, PASTA Theorem, The M/M/1 Queue, M/G/1 Queue, Reversed Chain, Reversible Queues, Networks of Queues, Chains with Matrix Geometric Solutions

# ACTIVITIES

## **Probability Review**

**Full-or-part-time:** 20h Theory classes: 4h Practical classes: 4h Self study: 12h



#### **Discrete time Markov Chains**

#### Specific objectives:

2, 3, 4

#### **Related competencies :**

CG1. Capability to apply the scientific method to study and analyse of phenomena and systems in any area of Computer Science, and in the conception, design and implementation of innovative and original solutions.

CG3. Capacity for mathematical modeling, calculation and experimental designing in technology and companies engineering centers, particularly in research and innovation in all areas of Computer Science.

CEE2.2. Capability to understand models, problems and algorithms related to computer networks and to design and evaluate algorithms, protocols and systems that process the complexity of computer communications networks.

CEE2.1. Capability to understand models, problems and algorithms related to distributed systems, and to design and evaluate algorithms and systems that process the distribution problems and provide distributed services.

CEE2.3. Capability to understand models, problems and mathematical tools to analyze, design and evaluate computer networks and distributed systems.

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Full-or-part-time: 60h

Theory classes: 12h Practical classes: 12h Self study: 36h

#### First assessment

**Full-or-part-time:** 12h Guided activities: 2h Self study: 10h

## **Continous time Markov chains**

Specific objectives:

2, 3, 4

## Related competencies :

CG1. Capability to apply the scientific method to study and analyse of phenomena and systems in any area of Computer Science, and in the conception, design and implementation of innovative and original solutions.

CG3. Capacity for mathematical modeling, calculation and experimental designing in technology and companies engineering centers, particularly in research and innovation in all areas of Computer Science.

CEE2.2. Capability to understand models, problems and algorithms related to computer networks and to design and evaluate algorithms, protocols and systems that process the complexity of computer communications networks.

CEE2.1. Capability to understand models, problems and algorithms related to distributed systems, and to design and evaluate algorithms and systems that process the distribution problems and provide distributed services.

CEE2.3. Capability to understand models, problems and mathematical tools to analyze, design and evaluate computer networks and distributed systems.

CTR6. REASONING: Capacity for critical, logical and mathematical reasoning. Capability to solve problems in their area of study. Capacity for abstraction: the capability to create and use models that reflect real situations. Capability to design and implement simple experiments, and analyze and interpret their results. Capacity for analysis, synthesis and evaluation.

Full-or-part-time: 32h Theory classes: 7h Practical classes: 4h Self study: 21h



#### Second assessment

Full-or-part-time: 12h Guided activities: 2h Self study: 10h

#### **Queueing theory**

Specific objectives: 2, 3, 4, 5

#### **Related competencies :**

CG1. Capability to apply the scientific method to study and analyse of phenomena and systems in any area of Computer Science, and in the conception, design and implementation of innovative and original solutions.

CG3. Capacity for mathematical modeling, calculation and experimental designing in technology and companies engineering centers, particularly in research and innovation in all areas of Computer Science.

CEE2.2. Capability to understand models, problems and algorithms related to computer networks and to design and evaluate algorithms, protocols and systems that process the complexity of computer communications networks.

CEE2.1. Capability to understand models, problems and algorithms related to distributed systems, and to design and evaluate algorithms and systems that process the distribution problems and provide distributed services.

CEE2.3. Capability to understand models, problems and mathematical tools to analyze, design and evaluate computer networks and distributed systems.

CTR6. REASONING: Capacity for critical, logical and mathematical reasoning. Capability to solve problems in their area of study. Capacity for abstraction: the capability to create and use models that reflect real situations. Capability to design and implement simple experiments, and analyze and interpret their results. Capacity for analysis, synthesis and evaluation.

Full-or-part-time: 26h Theory classes: 5h Practical classes: 6h Self study: 15h

# Final exam

Specific objectives:

2, 3, 4, 5

## Related competencies :

CG1. Capability to apply the scientific method to study and analyse of phenomena and systems in any area of Computer Science, and in the conception, design and implementation of innovative and original solutions.

CG3. Capacity for mathematical modeling, calculation and experimental designing in technology and companies engineering centers, particularly in research and innovation in all areas of Computer Science.

CEE2.2. Capability to understand models, problems and algorithms related to computer networks and to design and evaluate algorithms, protocols and systems that process the complexity of computer communications networks.

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CEE2.3. Capability to understand models, problems and mathematical tools to analyze, design and evaluate computer networks and distributed systems.

CTR6. REASONING: Capacity for critical, logical and mathematical reasoning. Capability to solve problems in their area of study. Capacity for abstraction: the capability to create and use models that reflect real situations. Capability to design and implement simple experiments, and analyze and interpret their results. Capacity for analysis, synthesis and evaluation.

Full-or-part-time: 17h

Guided activities: 2h Self study: 15h



# **GRADING SYSTEM**

The theory mark will be calculated from the problems delivered by the student, assessment marks and a final exam mark. The formula for calculating the mark for the course is:

NF = 0.1 \* NP + 0.15 \* max{EF, C1} + 0.15 \* max{EF, C2} + 0.60 \* EF

where:

NF = final mark

EF = final theory exam

 $\mathsf{NP}=\mathsf{Problems}$  delivered by the students

C1,C2 = marks of midterm assessments

# **BIBLIOGRAPHY**

## **Basic:**

- Nelson, R. Probability, stochastic processes, and queueing theory: the mathematics of computer performance modelling. Springer, 1995. ISBN 0387944524.

- Kemeny, J.G.; Snell, J.L. Finite markov chains. Springer-Verlag, 1976. ISBN 0387901922.

- Trivedi, K.S. Probability and statistics with reliability, queuing, and computer science applications. 2nd ed. John Wiley & Sons, 2001. ISBN 0471333417.

## **Complementary:**

- Feller, W. An introduction to probability theory and its applications: volume I. 3rd ed. John Wiley and Sons, 1968. ISBN 0471257117.