200111 - AMG - Multilinear Algebra and Geometry

Coordinating unit: 200 - FME - School of Mathematics and Statistics
Teaching unit: 749 - MAT - Department of Mathematics
Academic year: 2019
Degree: BACHELOR'S DEGREE IN MATHEMATICS (Syllabus 2009). (Teaching unit Compulsory)
ECTS credits: 7,5
Teaching languages: Catalan, Spanish

Teaching staff

Coordinator: PEDRO PASCUAL GAINZA
Others:
Primer quadrimestre:
FRANCESC XAVIER GRACIA SABATE - M-A
PEDRO PASCUAL GAINZA - CFIS, M-A, M-B
ENRIC VENTURA CAPELL - CFIS, M-B

Prior skills

Students must have achieved the objectives of Linear Algebra and Euclidean and Affine Geometry

Degree competences to which the subject contributes

Specific:
1. CE-2. Solve problems in Mathematics, through basic calculation skills, taking in account tools availability and the constraints of time and resources.
2. CE-3. Have the knowledge of specific programming languages and software.
3. CE-4. Have the ability to use computational tools as an aid to mathematical processes.

Generical:
4. CB-1. Demonstrate knowledge and understanding in Mathematics that is founded upon and extends that typically associated with Bachelor's level, and that provides a basis for originality in developing and applying ideas, often within a research context.
5. CB-2. Know how to apply their mathematical knowledge and understanding, and problem solving abilities in new or unfamiliar environments within broader or multidisciplinary contexts related to Mathematics.
6. CB-3. Have the ability to integrate knowledge and handle complexity, and formulate judgements with incomplete or limited information, but that include reflecting on social and ethical responsibilities linked to the application of their knowledge and judgements.
7. CG-1. Show knowledge and proficiency in the use of mathematical language.
8. CG-2. Construct rigorous proofs of some classical theorems in a variety of fields of Mathematics.
9. CG-3. Have the ability to define new mathematical objects in terms of others already know and ability to use these objects in different contexts.
10. CG-4. Translate into mathematical terms problems stated in non-mathematical language, and take advantage of this translation to solve them.
12. CG-6 Detect deficiencies in their own knowledge and pass them through critical reflection and choice of the best action to extend this knowledge.

Transversal:
11. SELF-DIRECTED LEARNING. Detecting gaps in one's knowledge and overcoming them through critical self-appraisal. Choosing the best path for broadening one's knowledge.
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**Teaching methodology**

(Section not available)

**Learning objectives of the subject**

(Section not available)

**Study load**

<table>
<thead>
<tr>
<th>Total learning time: 187h 30m</th>
<th>Hours large group: 45h</th>
<th>24.00%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Hours medium group:</td>
<td>0h</td>
<td>0.00%</td>
</tr>
<tr>
<td>Hours small group:</td>
<td>30h</td>
<td>16.00%</td>
</tr>
<tr>
<td>Guided activities:</td>
<td>0h</td>
<td>0.00%</td>
</tr>
<tr>
<td>Self study:</td>
<td>112h 30m</td>
<td>60.00%</td>
</tr>
</tbody>
</table>
# Content

## Jordan canonical form

**Learning time:** 5h  
Theory classes: 3h  
Laboratory classes: 2h

**Description:**  
We continue the analysis of square matrices begun in Linear Algebra studying the Jordan canonical form.

## Multilinear algebra

**Learning time:** 18h  
Theory classes: 11h  
Practical classes: 7h

**Description:**  
- Bilinear and quadratic forms.  
  - The vector space of tensors.  
  - Tensor product. Basis.  
  - Exterior product. Basis.

## Projective geometry

**Learning time:** 19h 10m  
Theory classes: 11h 40m  
Practical classes: 7h 30m

**Description:**  
- Projective space (real and complex).  
- Interpretations of projective plane.  
- Projective completion of an affine space.  
- Linear varieties. Grassmann.  
- Reference systems and projective coordinates. Equations of linear varieties.  
- Cross ratio.  
- Duality.  
  - Pappus and Desargues' theorems.  
  - Axiomatic definition of the projective plane. Non desarguesian planes.
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## Projectivities

**Learning time:** 18h  
Theory classes: 11h  
Laboratory classes: 7h

**Description:**  
- Projectivities and homographies. Properties.  
- The Main Theorem of Projective Geometry.  
- Matrices of projectivities.  
- Projectivities, linear varieties and duality.  
- Fixed points and fixed varieties.  
- Some families of projectivities: perspectivities, involutions and homologies. Poncelet’s Theorem.  
- Homographies of the line and the plane.  
- Affine maps as projectivities

## Quadrics

**Learning time:** 17h  
Theory classes: 10h  
Practical classes: 7h

**Description:**  
- Hyperquadrics of a projective space.  
- Polarity.  
- Projective classification of quadrics (real and complex).  
- Affine classification of quadrics (real and complex).  
- Conics. Steiner’s theorem.  
- Euclidean geometry inside projective geometry.

### Qualification system

The final mark of the subject will be obtained from a final exam (EF mark) and from a continuous assessment (AC) and a midterm exam (EP mark).

The final exam will consist of a part with some problems and a theoretical part.

The final subject mark will be the result of:

\[
\max \{ \text{EF} , 0.8 \text{EF} + 0.2 \text{EP} , 0.7 \text{EF} + 0.2 \text{EP} + 0.1 \text{AC} , 0.9 \text{EF} + 0.1 \text{AC} \}
\]

An extra exam will take place on July for students that failed during the regular semester.
Bibliography

Basic:


Complementary: