250102 - CÀLCUL - Calculus

Coordinating unit: 250 - ETSECCPB - Barcelona School of Civil Engineering
Teaching unit: 751 - DECA - Department of Civil and Environmental Engineering
Academic year: 2018
Degree: BACHELOR'S DEGREE IN CIVIL ENGINEERING (Syllabus 2010). (Teaching unit Compulsory)
BACHELOR'S DEGREE IN CIVIL ENGINEERING (Syllabus 2017). (Teaching unit Compulsory)
ECTS credits: 9
Teaching languages: Catalan, Spanish

Teaching staff
Coordinator: M. ROSA ESTELA CARBONELL
Others: ALBERT CREUS MIR, M. ROSA ESTELA CARBONELL, FRANCISCO JAVIER MARCOTE ORDAX, AGUSTIN MEDINA SIERRA, JAUME SOLER VILLANUEVA

Opening hours
Timetable: Tuesday from 10:00 am to 12:00 am C2-205 module and hours to be arranged with individual teachers. eConsultes online

Degree competences to which the subject contributes

Specific:
3048. Ability to solve the types of mathematical problems that may arise in engineering. Ability to apply knowledge of: linear algebra; geometry; differential geometry; differential and integral calculus; differential equations and partial derivatives; numerical methods; numerical algorithms; statistics and optimisation.
3049. Ability to select resources from knowledge of: linear algebra; geometry; differential geometry; differential and integral calculus; differential equations and partial derivatives; numerical methods; numerical algorithms; statistics and optimisation. All with a view to solving the types of mathematical problems that may arise in engineering

588. SUSTAINABILITY AND SOCIAL COMMITMENT - Level 1. Analyzing the world’s situation critically and systemically, while taking an interdisciplinary approach to sustainability and adhering to the principles of sustainable human development. Recognizing the social and environmental implications of a particular professional activity.
591. EFFICIENT ORAL AND WRITTEN COMMUNICATION - Level 1. Planning oral communication, answering questions properly and writing straightforward texts that are spelt correctly and are grammatically coherent.
598. EFFECTIVE USE OF INFORMATION RESOURCES - Level 2. Designing and executing a good strategy for advanced searches using specialized information resources, once the various parts of an academic document have been identified and bibliographical references provided. Choosing suitable information based on its relevance and quality.
601. SELF-DIRECTED LEARNING - Level 2: Completing set tasks based on the guidelines set by lecturers. Devoting the time needed to complete each task, including personal contributions and expanding on the recommended information sources.
250102 - CÀLCUL - Calculus

Teaching methodology

The course consists of 7 hours per week of classroom activity from beginning the of November to the end of the first four-month period. During the second quarter there are 3 hours a week of classroom. In the course there are theoretical lectures, in which the teacher presents the basic concepts and topics of the subject, shows examples and solves exercises and others with greater interaction with the students. The objective of these practical exercises is to consolidate the general and specific learning objectives. The course uses the "flipped classroom" methodology where the student, by means of specific group-dynamics techniques, extends and consolidates the knowledge acquired during the out-of-class preparation, in advance, of basic elements corresponding the following classes. The out-of-class preparation is carried out by the student, supported by videos, transparencies, books and bibliographic material, provided on the website of the course, and according to the directions of the teacher. Then, the in-class group dynamics consists of providing the group of students the required additional knowledge, according to the possible weaknesses identified by the teacher, perform practical exercises, answer questions, deepen the students knowledge on the subject and promote teamwork. Support material is provided through the virtual campus ATENEA in the form of detailed activity plans which include contents, learning programme, bibliography and assessment activities.

Learning objectives of the subject

Students will learn to perform differential and integral calculus of one variable and to apply these techniques to mathematical problems encountered in engineering.

On completion of the course, students will have acquired the ability to:
1. Relate ordinary differential equations to engineering problems, solve ODEs in simple conditions, and conduct analyses such as parametric studies to validate the solutions;
2. Solve engineering problems requiring minimisation, integration and analysis of functions of several variables;
3. Use Fourier series to solve engineering problems.

Differential calculus of functions of several variables; Integral calculus of several variables, including integral representation of functions and parameter-dependent integrals; Fourier series and their application to civil engineering problems; Ordinary differential equations

Study load

<table>
<thead>
<tr>
<th>Total learning time: 225h</th>
<th>Theory classes: 51h</th>
<th>22.67%</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Practical classes: 28h</td>
<td>12.44%</td>
</tr>
<tr>
<td></td>
<td>Laboratory classes: 11h</td>
<td>4.89%</td>
</tr>
<tr>
<td></td>
<td>Guided activities: 9h</td>
<td>4.00%</td>
</tr>
<tr>
<td></td>
<td>Self study: 126h</td>
<td>56.00%</td>
</tr>
</tbody>
</table>
**Content**

### Topic 1. Metric spaces. Topology

**Learning time:** 7h 11m  
  - Theory classes: 2h  
  - Practical classes: 1h  
  - Self study: 4h 11m

**Description:**  
Topology. Basics  
Difficulties in consolidating the concepts 1.5h  assessment test 0.5h

<table>
<thead>
<tr>
<th>Item 2. Numerical successions and series</th>
<th>Learning time: 24h</th>
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</thead>
<tbody>
<tr>
<td>Theory classes: 6h</td>
<td>Practical classes: 3h</td>
</tr>
<tr>
<td>Laboratory classes: 1h</td>
<td>Self study: 14h</td>
</tr>
</tbody>
</table>

**Description:**  
Problems sequences and series  
Test

<table>
<thead>
<tr>
<th>Item 3. Differential calculus of real functions of real variable</th>
<th>Learning time: 19h 12m</th>
</tr>
</thead>
<tbody>
<tr>
<td>Theory classes: 4h</td>
<td>Practical classes: 3h</td>
</tr>
<tr>
<td>Laboratory classes: 1h</td>
<td>Self study: 11h 12m</td>
</tr>
</tbody>
</table>

**Description:**  
Achievement of the concepts  
Test
## Item 4. Differential calculus of functions of several variables

**Learning time:** 57h 35m

<table>
<thead>
<tr>
<th>Theory classes:</th>
<th>13h</th>
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</thead>
<tbody>
<tr>
<td>Practical classes:</td>
<td>7h</td>
</tr>
<tr>
<td>Laboratory classes:</td>
<td>4h</td>
</tr>
<tr>
<td>Self study:</td>
<td>33h 35m</td>
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</tbody>
</table>

**Description:**
- Limits and continuity of functions of several variables.
- Partial and directional derivative.
- The differential of a function.
- Sufficient condition for differentiability.
- Chain rule.
- Inverse and implicit function theorems.
- Higher order derivatives.
- Schwarz's theorem.
- Taylor's theorem.
- Local and conditional extrema.
- Consolidation of concepts
- Test

## Item 5. Riemann

**Learning time:** 16h 48m

<table>
<thead>
<tr>
<th>Theory classes:</th>
<th>4h</th>
</tr>
</thead>
<tbody>
<tr>
<td>Practical classes:</td>
<td>2h</td>
</tr>
<tr>
<td>Laboratory classes:</td>
<td>1h</td>
</tr>
<tr>
<td>Self study:</td>
<td>9h 48m</td>
</tr>
</tbody>
</table>

**Description:**
- Upper and lower integral.
- Definition of Riemann integral.
- Properties.
- Riemann-integrable functions.
- Lebesgue theorem.
- Primitive concept.
- The integral function.
- Integration and differentiation.
- Fundamental theorem of calculus.
- Barrow's rule.
- Mean value theorem.
- Substitution theorem.
- Integration by parts.
- Improper integrals.
- Applications of the integral.
- Problems
- Test

## Item 6. Riemann integral multiple

**Learning time:** 24h

<table>
<thead>
<tr>
<th>Theory classes:</th>
<th>6h</th>
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<tbody>
<tr>
<td>Practical classes:</td>
<td>3h</td>
</tr>
<tr>
<td>Laboratory classes:</td>
<td>1h</td>
</tr>
<tr>
<td>Self study:</td>
<td>14h</td>
</tr>
</tbody>
</table>

**Description:**
- Upper and lower integral.
- Multiple Riemann integral.
- Lebesgue criterion.
- Repeated one-dimensional integration.
- Fubini's theorem.
- Jordan measurable sets.
- Change of variables theorem.
- Integral representation of functions.
- Integrals depending on a parameter.
- Problems
- Test
### Item 7. Sequences and Functional Series. Fourier Series

**Learning time:** 14h 23m  
Theory classes: 3h  
Practical classes: 2h  
Laboratory classes: 1h  
Self study: 8h 23m

**Description:**  
Problems  
Consolidation of concepts

### Item 8. Ordinary Differential Equations

**Learning time:** 52h 48m  
Theory classes: 11h  
Practical classes: 6h  
Laboratory classes: 5h  
Self study: 30h 48m

**Description:**  
Problems. Solving differential equations and systems of ODEs.  
Laboratories resolution of ODEs and systems  
Test
Qualification system

The final mark is a number in the 0 – 10 range, 0 being the lowest possible mark. Pass mark is 5. The final mark $N_{\text{final}}$ is given by

$$N_{\text{final}} = 0.4 \times N_c + 0.3 \times N_{\text{pg}1} + 0.3 \times N_{\text{pg}2}$$

where $N_c$ is the mark received from continuous assessment in class activities and $N_{\text{pg}1}$ and $N_{\text{pg}2}$ are the mark received in the global exams.

Continuous assessment consists of several activities, either individual or in group, carried out during the academic year (either in or out of the classroom).

The final exam is intended to check the student’s knowledge and understanding of the mathematical concepts studied during the course. It contains a number of questions on concepts related to the learning outcomes and a number of application exercises.

Students who have failed the course but have been passing regularly the continuous assessment tests at the end of each block are eligible for a reassessment exam, which will take place on the date announced in the academic calendar. The highest final mark attainable in the case of reassessment is the pass mark 5.

Students who cannot be assessed due to justifiable absence from lectures or exams can sit the reassessment exam only by special permission of the Head of Studies. In this case, the limitation of 5 on the highest attainable mark will not apply to the blocks assessed for the first time.

Criteria for re-evaluation qualification and eligibility: Students that failed the ordinary evaluation and have regularly attended all evaluation tests will have the opportunity of carrying out a re-evaluation test during the period specified in the academic calendar. Students who have already passed the test or were qualified as non-attending will not be admitted to the re-evaluation test. The maximum mark for the re-evaluation exam will be five over ten (5.0). The non-attendance of a student to the re-evaluation test, in the date specified will not grant access to further re-evaluation tests. Students unable to attend any of the continuous assessment tests due to certifiable force majeure will be ensured extraordinary evaluation periods.

These tests must be authorized by the corresponding Head of Studies, at the request of the professor responsible for the course, and will be carried out within the corresponding academic period.

Regulations for carrying out activities

Failure to sit a continuous assessment exam or to hand in an assignment before its deadline will result in a mark of 0 in this exam or assignment.
## Bibliography

### Basic:


### Complementary:


