Course guide
820007 - CAL - Calculus

Unit in charge: Barcelona East School of Engineering
Teaching unit: 749 - MAT - Department of Mathematics.

Degree:
BACHELOR'S DEGREE IN BIOMEDICAL ENGINEERING (Syllabus 2009). (Compulsory subject).
BACHELOR'S DEGREE IN CHEMICAL ENGINEERING (Syllabus 2009). (Compulsory subject).
BACHELOR'S DEGREE IN ELECTRICAL ENGINEERING (Syllabus 2009). (Compulsory subject).
BACHELOR'S DEGREE IN ENERGY ENGINEERING (Syllabus 2009). (Compulsory subject).
BACHELOR'S DEGREE IN INDUSTRIAL ELECTRONICS AND AUTOMATIC CONTROL ENGINEERING (Syllabus 2009). (Compulsory subject).
BACHELOR'S DEGREE IN MECHANICAL ENGINEERING (Syllabus 2009). (Compulsory subject).
BACHELOR'S DEGREE IN MATERIALS ENGINEERING (Syllabus 2010). (Compulsory subject).

Academic year: 2023 ECTS Credits: 6.0 Languages: Catalan, Spanish, English

LECTURER

Coordinating lecturer: ANGELES CARMONA MEJIAS - MAGDA LILIANA RUIZ ORDOÑEZ

Others:

Primer quadrimestre:
ENRIC AMADO VICENTE - Grup: T21, Grup: T22, Grup: T23
ANGELES CARMONA MEJIAS - Grup: M51, Grup: M52
MERCÉ CLAVEROL AGUAS - Grup: M21, Grup: M22, Grup: M42, Grup: M52, Grup: M81, Grup: M82, Grup: M91
ADRIÁN DOMINGO GIMENEZ - Grup: X22
RAIMON ELGUETA MONTO - Grup: X11, Grup: X12, Grup: X22
ANDRES MARCOS ENCINAS BACHILLER - Grup: M71, Grup: M72
ALFONSO ESCOBOSA FERNANDEZ - Grup: T11, Grup: T12
MARIONA GONZÁLEZ ESTEVE - Grup: T12, Grup: T22, Grup: X11, Grup: X21
SERGIO GONZÁLEZ LÓPEZ - Grup: M31, Grup: M41, Grup: M42, Grup: M72, Grup: X21, Grup: X22
NILS GUTIÉRREZ VON PORAT - Grup: M81
PERE LOPEZ BROSA - Grup: M61
ALBERT MAS BLESA - Grup: M31, Grup: M41, Grup: M42, Grup: M72, Grup: X21, Grup: X22
NURIA PARES MARINE - Grup: M11, Grup: M32, Grup: M71
FRANCESC POZO MONTERO - Grup: M11
JOAN QUINTANA COMPTE - Grup: M41, Grup: M51, Grup: M52, Grup: M91, Grup: M92
MAGDA LILIANA RUIZ ORDOÑEZ - Grup: M21, Grup: M61, Grup: M62, Grup: M92
ROGER VALDÉS I MARTÍN - Grup: M22, Grup: M31, Grup: M32

Segon quadrimestre:
ENRIC AMADO VICENTE - Grup: T11, Grup: T12, Grup: T21, Grup: T22
ANGELES CARMONA MEJIAS - Grup: M21, Grup: M22, Grup: M31, Grup: M32
MERCÉ CLAVEROL AGUAS - Grup: M11
ADRIAN DOMINGO GIMENEZ - Grup: T22
ANDRES MARCOS ENCINAS BACHILLER - Grup: M21, Grup: M22
ALFONSO ESCOBOSA FERNANDEZ - Grup: T11, Grup: T12, Grup: T21, Grup: T22
CÉCILIA OLIVESI - Grup: M12
MAGDA LILIANA RUIZ ORDOÑEZ - Grup: M11, Grup: M12, Grup: M31, Grup: M32

PRIOR SKILLS

This course requires no previous skills.
REQUIREMENTS

This course has no prerequisites.

DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES

Specific:
2. Solve mathematical problems that may arise in engineering. Apply knowledge of linear algebra; geometry; differential geometry; differential and integral calculus; differential equations and partial differential equations; numerical methods; numerical algorithms; statistics and optimisation.

Transversal:
1. SELF-DIRECTED LEARNING - Level 1. Completing set tasks within established deadlines. Working with recommended information sources according to the guidelines set by lecturers.

TEACHING METHODOLOGY

The course uses the expositive methodology by 40% and individual work by 60%.

LEARNING OBJECTIVES OF THE SUBJECT

General objectives: Students will learn the fundamental concepts of single variable calculus, developing the capacity of abstraction and applying these techniques to mathematical problems encountered in engineering.

STUDY LOAD

<table>
<thead>
<tr>
<th>Type</th>
<th>Hours</th>
<th>Percentage</th>
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<tbody>
<tr>
<td>Hours small group</td>
<td>15,0</td>
<td>10.00</td>
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<tr>
<td>Hours large group</td>
<td>45,0</td>
<td>30.00</td>
</tr>
<tr>
<td>Self study</td>
<td>90,0</td>
<td>60.00</td>
</tr>
</tbody>
</table>

Total learning time: 150 h
## CONTENTS

### Sets of numbers

**Description:**
- The set of real numbers: Supremum axiom.
Euler's formula. Definition of hyperbolic functions and their relation to trigonometry and complex numbers.

**Specific objectives:**
The students will learn:
- Supremum axiom, key to understand the completeness of real numbers.
- to operate with complex numbers.
- to establish relationships between binomial, polar, and exponentials forms.

**Related activities:**
Lab session 1. Conics
Lab session 2. Complex numbers

**Full-or-part-time:** 30h
- Theory classes: 8h
- Laboratory classes: 4h
- Self study: 18h

### Functions of real variable. Limits and continuity.

**Description:**
- Continuity. Continuity theorems (Weierstrass, Bolzano, intermediate value theorem).

**Specific objectives:**
Students will learn:
- to represent a real-valued function.
- to understand the importance of the concept of limit and its relationship to continuity.

**Related activities:**
Lab Session 3. Limits and continuity

**Full-or-part-time:** 30h
- Theory classes: 10h
- Laboratory classes: 2h
- Self study: 18h
**Differentiation of real-valued functions**

**Description:**
- Mean value theorems (Rolle, Cauchy, Lagrange).
- Extrema of a function in an interval.

**Specific objectives:**
The student will learn:
- the basic concepts of differentiation.
- to understand the geometric interpretation of the derivative and its applications in engineering.
- to master and apply the elementary properties of the differentiable functions.
- to master the computation of derivatives, both analytically and with the help of mathematical software.
- to model and solve several problems by computing derivatives: optimization, approximation of functions, and qualitative study of functions.

**Related activities:**
Lab session 6. PART I: Taylor polynomial

**Full-or-part-time:** 35h
Theory classes: 12h
Laboratory classes: 2h
Self study : 21h

**Integration of real-value functions**

**Description:**
- Primitive functions.
- Integration methods: direct methods, change of variable, integration by parts, trigonometric integrals.
- Computation of areas of plane regions. Applications.
- Improper integrals.

**Specific objectives:**
Students will learn:
- to express in terms of integrals the problem of computing the area of a plane region.
- to understand the relationship between derivatives and integrals, given by the fundamental theorem of calculus.
- to use the Barrow’s rule.
- to compute some improper integrals of continuous functions on an unbounded interval, and improper integrals of functions with a singularity inside a bounded interval.

**Related activities:**
Lab session 6. PART II: Integration
Lab session 7. Lab session exam (10%)

**Full-or-part-time:** 42h
Theory classes: 13h
Laboratory classes: 3h
Self study : 26h
Linear algebra

Description:
Systems of linear equations. Gaussian elimination.
Inverse matrix.
Linear geometry: equation of a straight line and a plane; orthogonality and parallelism; distances.

Specific objectives:
Students will learn:
-to solve systems of linear equations.
-to graphically represent the solution of a system of linear equations.

Related activities:
Lab Session 4. Matrices
Lab Session 5. Generic competence assessment

Full-or-part-time: 15h
Theory classes: 2h
Laboratory classes: 4h
Self study : 9h

GRADING SYSTEM
First partial exam: 35% (Test+Exercise)
Second partial exam: 45% (Test+Exercises)
Laboratory exam with MAPLE: 10%
Generic competence:10%

Students can pass the course through the continuous assessment based on two exams (a first mid course exam and a second exam during the period fixed in the academic calendar of the school devoted to the final exams) and the delivery of laboratory assessments. Finally, as detailed in the academic normative of the EEBE, a reevaluation exam will take place (excluding the MAPLE Laboratory exam and the Generic Competence). To be able to do the reevaluation exam, the student has to attend to all the evaluation exams of the subject and its mark, N, for the part which can be reevaluated has to be such that 3.0

An individual test will be performed in the assessment of the laboratory, during the last laboratory session, and another test will evaluate the generic competency. This course assesses the self-directed learning competency through individual tests during the development of one of the laboratory sessions. More precisely, the test will assess conics.

EXAMINATION RULES.

No writing paper, books, papers, manuscripts, or notes of any kind are allowed to be taken into an examination room. The use of calculators, cell phones, tablets, or any electronic device is not permitted during the exams.
BIBLIOGRAPHY

Basic:

Complementary:

RESOURCES

Hyperlink:
- Khan Academy. Resource

Other resources:
Web page: https://es.khanacademy.org