

## 220332 - Astrodynamics

Coordinating unit:	205 - ESEIAAT - Terrassa School of Industrial, Aerospace and Audiovisual Engineering		
Teaching unit:	220 - ETSEIAT - Terrassa School of Industrial and Aeronautical Engineering		
Academic year:	2018		
Degree:	MASTER'S DEGREE IN AERONAUTICAL ENGINEERING (Syllabus 2014). (Teaching unit Optional) MASTER'S DEGREE IN SPACE AND AERONAUTICAL ENGINEERING (Syllabus 2016). (Teaching unit Optional)		
ECTS credits:	5	Teaching languages:	English

### Teaching staff

Coordinator:	De La Torre Sangrà, David
Others:	De La Torre Sangrà, David

### Opening hours

Timetable:	To be defined
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### Prior skills

The student must have background knowledge of algebra, geometry, calculus, programming, basic physics (dynamics of point masses), basics orbital mechanics (two-body problem, Keplerian orbits, main perturbations produced by J2 according to first-order theory, orbital elements, patched conics, gravity assist, Hohmann transfer, basic impulsive maneuvers, launch geometry).

### Requirements

The following subjects of the Degree are a prerequisite for this course: Calculus I, Linear Algebra, Physics I, Mechanics, Software Engineering, Space Engineering (or Introduction to Space Engineering of the first year of MUEA). The following subjects of MUEA are also a requirement: Aerodynamics, Flight and Orbital Mechanics and Software Engineering.

### Degree competences to which the subject contributes

Specific:

CB06. Manage original concepts in research projects.

CB10. Improve self-learning capacity

CEEESPAC1. MUEA/MASE: Sufficient applied knowledge of the planning of space missions (specific competency for the specialisation in Space).

CEEESPAC2. MUEA/MASE: Advanced applied knowledge of orbital dynamics and space vehicle design (specific competency for the specialisation in Space).

CG06-MUEA. (ENG) Capacitat per a l'anàlisi i la resolució de problemes aeroespacials en entorns nous o desconeguts, dins de contextos amplis i complexos.

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### Teaching methodology

Lectures consist in classes with theoretical content (in which the participation of the students is sought) and application sessions whose contents are exercises and simulations made with computer codes (either in Fortran language or in the Matlab environment) which allow the student to understand and assimilate the theoretical concepts. It is important that the students repeat the exercises on their own by trying different cases. All the proposed codes lend themselves to modification and further implementation, activities which stimulate the creativity and the interest in investigation.

### Learning objectives of the subject

The learning objectives of this subject consist in the development of the following skills:

Ability to analyze the geometry of an orbit and its effects on the objectives of the mission.

Ability to understand and develop a Delta-V (or amount of fuel) budget.

Ability to solve Lambert's problem (approach, selection of solution method, solution by iterative numerical algorithm, expression of the result in a form suitable for use in the description of the motion).

Ability to study a planet-to-planet direct transfer and analyze the corresponding launch opportunities through the so-called Pork Chop Plot (PCP).

Ability to determine the effects of a planetary gravity assist: given the initial heliocentric orbital elements, determine the effects of interaction with the given planet.

Ability to calculate and interpret the Tisserand graph.

Ability to distinguish among different optimization methods and their domains of applicability.

Basic knowledge of the circular restricted problem of three bodies, their characteristics and peculiarities, their astrodynamical applications.

Basic knowledge of design of low-thrust trajectory.

### Study load

Total learning time: 125h	Hours large group:	30h	24.00%
	Hours small group:	15h	12.00%
	Self study:	80h	64.00%

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### Content

#### MODULE 1 - GEOCENTRIC ORBITS

Learning time: 27h

Theory classes: 7h  
Laboratory classes: 3h  
Self study : 17h

##### Description:

This module consists in the following:

- Short reminder of fundamentals of orbital mechanics.
- Geocentric missions:
  - selection of orbital parameters versus mission objectives;
  - geometrical characteristics (groundtrack, coverage, azimuth-elevation, swath width, revisit time);
  - special orbits (Molniya, Tundra, geosynchronous, heliosynchronous, geostationary with the perturbations due to J22);
  - constellations (Walker code) and their characterization.

##### Related activities:

Activities 1 and 2

#### MODULE 2 - LAMBERT'S PROBLEM

Learning time: 23h

Theory classes: 5h  
Laboratory classes: 3h  
Self study : 15h

##### Description:

The problem of Lambert, also known as the two-point boundary value problem, is a classical one in astrodynamics and celestial mechanics. Its importance is due to its central role in a large number of issues. This is why it is assigned an entire module in this course. The topic will be addressed following a traditional approach:

- Problem definition, statement of the theorem of Lambert, sketch of proof
- Numerical aspects of the problem
- Classical methods of solution (Lagrange , Gauss) with exercises
- Introduction to modern methods
- Application to the problem of interplanetary transfer. Examples
- Employment for studying the opportunities for such transfers. Examples.
- Pork Chop Plot (PCP)

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<b>MODULE 3 - INTERPLANETARY TRAJECTORIES</b>	Learning time: 33h Theory classes: 8h Laboratory classes: 4h Self study : 21h
Description: <ul style="list-style-type: none"> <li>- Discussion on dynamical models : two-body problem, N-body probm, patched conics</li> <li>- Rigorous definition of gravitational sphere of influence (SOI)</li> <li>- Calculation of the intersection of a planet-to-planet trajectory with the planetary SOI</li> <li>- Physics of the gravitaty assist (swingby) in 2D and 3D</li> <li>- Effects of gravity assist on the heliocentric orbital elements</li> <li>- Characterization of the planets as good or bad accelerators. Examples.</li> <li>- Introduction to the optimization of interplanetary trajectories</li> </ul>	
<b>MODULE 4 - THE THREE-BODY PROBLEM</b>	Learning time: 23h Theory classes: 6h Laboratory classes: 3h Self study : 14h
Description: The three-body problem in the discussion on the dynamical systems and their approximations. General problem of three bodies. <ul style="list-style-type: none"> <li>- Approximation: the circular restricted problem of three bodies.</li> <li>- Dynamical equations in the synodic reference frame, equilibria, Jacobi constant, zero velocity surfaces</li> <li>- Linear stability of the equilibrium points</li> <li>- Periodic and non-periodic orbits around the collinear points</li> <li>- Invariant manifolds</li> <li>- Application to the study of trajectories of small bodies and space missions.</li> </ul>	
<b>MODULE 5 - INTRODUCTION TO THE DESIGN OF LOW-THRUST TRAJECTORIES</b>	Learning time: 19h Theory classes: 4h Laboratory classes: 2h Self study : 13h
Description: Low-thrust trajectories (electric propulsion or solar sail) as control problems. Introduction to optimal control theory: <ul style="list-style-type: none"> <li>- Principle of Pontryagin</li> <li>- Types of boundary conditions</li> <li>- Analysis and solution of simple cases</li> </ul> Importance in Astrodynamics. Applications	

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### Qualification system

The final grade is computed by means of the following formula :

$$G (\text{final}) = 0.1 * G (\text{DE1}) + 0.1 * G (\text{DE2}) + 0.4 * G (\text{PRJ}) + 0.4 * G (\text{FEX})$$

where G means grade and

DE1 = deliverable exercise

DE2 = deliverable exercise

PRJ = course project

FEX = final exam

More information in the Activities section.

For those students who meet the requirements and submit to the reevaluation examination, the grade of the reevaluation exam will replace the grades of all the on-site written evaluation acts (tests, midterm and final exams) and the grades obtained during the course for lab practices, works, projects and presentations will be kept.

If the final grade after reevaluation is lower than 5.0, it will replace the initial one only if it is higher. If the final grade after reevaluation is greater or equal to 5.0, the final grade of the subject will be pass 5.0.

### Regulations for carrying out activities

In the in-class exams (i.e., FEX) lecture notes, slides and formula sheets are not permitted. The use of non-programable calculator is allowed. The duration of each in-class exam is of one hour. The exam done from home (i.e., DE1 and DE2) must be carried out individually: the students will receive the text of the exam through Atenea and will be given a deadline (typically of a few days, the exact time depending on the characteristics of the assignment) for the delivery of a computer code that solves the proposed problem and a report that illustrates it.

### Bibliography

Basic:

Bate, R. R.; Mueller, D. D.; White, J. E. Fundamentals of astrodynamics. New York: Dover, 1971. ISBN 9780486600611.

Battin, Richard H. An introduction to mathematics and methods of astrodynamics. Rev. ed. Virginia: American Institute of Aeronautics and Astronautics, 1999. ISBN 1563473429.

Kaplan, Marshall H. Modern spacecraft dynamics & control. New York: Wiley, 1976. ISBN 0417457035.

Wertz, J. R.; Larson, W. J. Space mission analysis and design. 3rd ed. Dordrecht [etc.]: Kluwer Academic, 1999. ISBN 9781881883104.