

## Course guides

### 295104 - 295II014 - Systems Modeling

Last modified: 04/06/2021

**Unit in charge:** Barcelona East School of Engineering  
**Teaching unit:** 729 - MF - Department of Fluid Mechanics.

**Degree:** MASTER'S DEGREE IN INTERDISCIPLINARY AND INNOVATIVE ENGINEERING (Syllabus 2019). (Compulsory subject).  
MASTER'S DEGREE IN MATERIALS SCIENCE AND ADVANCED MATERIALS ENGINEERING (Syllabus 2019). (Optional subject).

**Academic year:** 2021    **ECTS Credits:** 6.0    **Languages:** English

#### LECTURER

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**Coordinating lecturer:** RICARDO JAVIER PRINCIPE RUBIO

**Others:** Primer quadrimestre:  
RICARDO JAVIER PRINCIPE RUBIO - T11, T12  
ALFREDO DE JESUS GUARDO ZABALETA - T11, T12

#### PRIOR SKILLS

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Calculus. Basic knowledge of differential equations.  
Fluid mechanics, heat transfer.  
Computer usage, notions of programming

#### DEGREE COMPETENCES TO WHICH THE SUBJECT CONTRIBUTES

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**Specific:**

CEMUEII-04. Design and implement modeling techniques to describe the operation of a system. Predict its stability and apply control techniques in different scenarios.

**Generical:**

CGMUEII-01. Participate in technological innovation projects in multidisciplinary problems, applying mathematical, analytical, scientific, instrumental, technological and management knowledge.

**Transversal:**

05 TEQ. TEAMWORK. Being able to work as a team player, either as a member or as a leader. Contributing to projects pragmatically and responsibly, by reaching commitments in accordance to the resources that are available.  
06 URI. EFFECTIVE USE OF INFORMATION RESOURCES. Managing the acquisition, structure, analysis and display of information from the own field of specialization. Taking a critical stance with regard to the results obtained.  
03 TLG. THIRD LANGUAGE. Learning a third language, preferably English, to a degree of oral and written fluency that fits in with the future needs of the graduates of each course.

#### TEACHING METHODOLOGY

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The hours of driven activities in large groups will be theoretical classes with an expository and participatory approach.  
The hours of activities directed in small groups will be devoted to the resolution of exercises and the computational simulations systems (in computer rooms) using commercial and open source software.  
The hours of autonomous learning will be devoted to the study of theory, the solution of problems and computer simulations of systems.



## LEARNING OBJECTIVES OF THE SUBJECT

- Understand models of physical systems based on partial differential equations, continuum mechanics and constitutive models.
- Understand the concept of weak solutions of partial differential equations, which are key to describe several physical phenomena (e.g. shock waves).
- Understand the concept of regularity of these solutions and how it determines the difficulty of the problem (e.g. the computational cost of numerical simulations).
- Understand the weak formulation of physical laws and the continuity conditions they imply when dealing with multiphysics problems.
- Identify multi-scale features of physical problems, select appropriate scale separation operators and small scale models.

## STUDY LOAD

Type	Hours	Percentage
Hours large group	34,0	22.67
Self study	96,0	64.00
Hours small group	20,0	13.33

**Total learning time:** 150 h

## CONTENTS

### Mathematical modeling of systems

**Description:**

Introduction to systems modeling  
Description of systems  
Constitutive modeling  
Some simple models

**Specific objectives:**

Understand different levels of descriptions of physical systems and strategies for their modeling.  
Learn continuum mechanics basis, constitutive modeling and possible simplifications.

**Related activities:**

A1 Computational modeling of laminar flows (flow past a cylinder, airfoil, driven cavity, etc.)

**Full-or-part-time:** 20h

Theory classes: 6h  
Laboratory classes: 2h  
Self study : 12h



### Classical theory of partial differential equations

**Description:**

Introduction to partial differential equations  
First and second order partial differential equations  
Fundamental solutions and their properties  
Green identities and Green functions

**Specific objectives:**

Learn basic concepts of partial differential equations (order, linearity, type)  
Understand properties of classical solutions (uniqueness, mean value, maximum principle, etc.), including regularity.

**Related activities:**

B1 Computational modeling of partial differential equations with regular solutions

**Full-or-part-time:** 42h

Theory classes: 10h  
Laboratory classes: 2h  
Self study : 30h

### General theory of partial differential equations

**Description:**

Nonlinear first order partial differential equations, shock waves  
Distributions and weak derivatives  
Functional spaces and weak formulation of partial differential equations  
Numerical methods for partial differential equations

**Specific objectives:**

Understand the need for generalized solutions of partial differential equations  
Learn the basis of weak derivatives, functional spaces and weak formulations  
Understand the impact of regularity on the computational cost of numerical methods

**Related activities:**

B2 Computational modeling of partial differential equations with non-regular (weak) solutions  
A2 Computational modeling of compressible flows (shock waves)

**Full-or-part-time:** 46h

Theory classes: 10h  
Laboratory classes: 6h  
Self study : 30h



## Multiphysics and multiscale modeling

### Description:

Transmission conditions in continuum mechanics.  
Classical homogenization theory  
Scale separation for nonlinear problems and small scale modeling

### Specific objectives:

- Understand continuity conditions implied by the weak formulation of physical laws
- Identify multiscale features of physical problems and learn the basics of scale separation and small scale modeling
- Choose appropriate solution strategies for multiscale problems

### Related activities:

A3 Computational modeling of fluid-structure interaction (airfoils, blood flows, aneurysms)  
B3 Computational modeling of partial differential equations with multiscale features  
A4 Computational modeling of turbulent flows

### Full-or-part-time: 42h

Theory classes: 8h  
Laboratory classes: 10h  
Self study : 24h

## GRADING SYSTEM

20% Basic computational lab sessions  
20% Applications to systems modelling  
20% Deliverable homeworks  
40% Final exam

## EXAMINATION RULES.

Individual exam; homeworks in groups of two people.

## BIBLIOGRAPHY

### Basic:

- Pope, S. B. Turbulent flows. Cambridge [etc.]: Cambridge University Press, 2000. ISBN 0521591252.
- Batchelor, G. K. An introduction to fluid dynamics. Cambridge: Cambridge University Press, 1973. ISBN 0521663962.
- Pavliotis, Grigorios A; Stuart, Andrew M. Multiscale methods : averaging and homogenization [on line]. New York, NY: Springer New York, 2008 [Consultation: 24/04/2020]. Available on: <http://dx.doi.org/10.1007/978-0-387-73829-1>. ISBN 9780387738291.
- Strauss, Walter A. Partial differential equations : an introduction. 2nd ed. Hoboken: John Wiley & Sons, 2008. ISBN 9780470054567.
- Evans, Lawrence C. Partial differential equations. 2nd ed. Providence, Rhode Island: American Mathematical Society, cop. 2010. ISBN 9780821849743.
- Ljung, Lennart; Glad, Torkel. Modeling of dynamic systems. Englewood Cliffs: PTR Prentice Hall, 1994. ISBN 0135970970.

### Complementary:

- Malvern, Lawrence E. Introduction to the mechanics of a continuous medium. Englewood Cliffs, NJ: Prentice-Hall, cop. 1969. ISBN 9780134876030.
- Wilcox, David C. Turbulence modelling for CFD. 3rd ed. La Canada, Calif.: DCW Industries, cop. 2006. ISBN 9781928729082.